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# High-pressure crystallography of rhombohedral PrAlO<sub>3</sub> perovskite

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## Abstract

The evolution of the crystal structure of rhombohedral PrAlO<sub>3</sub> perovskite with pressure has been investigated by single-crystal x-ray diffraction and Raman scattering experiments. The structural evolution as indicated by lattice strains, octahedral tilts, and the distortions of the octahedral AlO<sub>6</sub> and polyhedral PrO<sub>12</sub> groups with increasing pressure, is controlled by the relative compressibilities of the AlO<sub>6</sub> octahedra and the PrO<sub>12</sub> site. Because the AlO<sub>6</sub> octahedra are more compressible than the PrO<sub>12</sub> sites, up to 7.4 GPa the structure evolves towards the high-symmetry cubic phase like any other rhombohedral perovskite. The variation of volume of the rhombohedral phase with pressure can be represented by a third-order Birch–Murnaghan equation of state with bulk modulus  $K_0 = 193.0(1.2)$  GPa and  $K' = 6.6(4)$ . Above 7.4 GPa the evolution towards a cubic phase is interrupted by a phase transition. Observations are consistent with the assignment of *Imma* symmetry to the high-pressure phase. Comparison with the low-temperature *R3c* to *Imma* transition confirms that electronic interactions stabilize the *Imma* phase.

## 1. Introduction

Structural phase transitions in perovskites that involve both octahedral tilting and cation displacements are the basis of many ferroelectric materials. The high-pressure phase transition behavior of ferroelectric perovskites should, in principal, provide important insights into the interactions that control the commercially important properties of these materials. For example, high pressure can be used to suppress the dynamics of chemically and micro-structurally complex relaxor ferroelectrics and allow the tilt transitions to be characterized in more detail than is possible at ambient pressures (Mihailova *et al* 2008). Yet, in structurally simpler perovskites such as PbTiO<sub>3</sub>, in which the symmetry rules for the possible phase transitions are constrained by theory (Howard and Stokes 2005), the phase transition sequence itself at high pressures remains a matter of experimental controversy

(Ahart *et al* 2008, Janolin *et al* 2008) and the mechanisms uncertain (Frantti *et al* 2007). This is surprising given that the structures of perovskites are simple enough for conceptual understanding at the crystal-chemical level, but have just enough degrees of freedom (Hammonds *et al* 1998) to enable them to display complex transition behavior.

Of the perovskites, those with *R3c* symmetry provide an ideal model system because the structure can be described in terms of just three free parameters; two cell parameters and one variable fractional coordinate of the oxygen atom. The positions of the octahedral cation, B, and the extra-framework (nominally 12-coordinate) A cation are fixed on symmetry positions. Nonetheless the symmetry constraints do allow the octahedra to tilt around one axis, to compress, and to distort, as in other perovskite space groups (Megaw and Darlington 1975). In the hexagonal setting of the unit-cell, the A cation is at (0, 0, 1/4), the B cation is at (0, 0, 0), and the oxygen is at

$(x, 0, 1/4)$ . The tilt angle  $\omega$  of the octahedra around the three-fold axis is given by (Megaw and Darlington 1975):

$$\omega = \arctan[2\sqrt{3}(x - 0.5)]. \quad (1)$$

The tilt angle becomes zero in the cubic aristotype phase with  $Pm\bar{3}m$  symmetry which can be achieved at high temperatures (Howard *et al* 2000). The tilt angle can also be expressed in terms of the ratio of the polyhedral volumes as (Thomas 1996):

$$V_A/V_B = 6\cos^2\omega - 1. \quad (2)$$

Differentiation of this equation shows that changes in the tilt of the octahedra with pressure are therefore controlled by the difference in volume compressibility ( $\beta_B - \beta_A$ ) between the  $BO_6$  octahedra and  $AO_{12}$  polyhedra (Zhao *et al* 2004b):

$$\frac{d\omega}{dP} = -\frac{6\cos^2\omega - 1}{6\sin 2\omega}(\beta_B - \beta_A). \quad (3)$$

On the basis of bond-valence theory, it can be shown (Zhao *et al* 2004a) that in a perovskite with cations with formal charge +3 the  $BO_6$  octahedra are more compressible than the extra-framework  $AO_{12}$  polyhedra. That is,  $(\beta_B - \beta_A) > 0$  and the tilt angle  $\omega$  of  $R\bar{3}c$  perovskites should decrease with increasing pressure, meaning that the structure should evolve towards cubic symmetry. This has been observed experimentally for  $LaAlO_3$  (Bouvier and Kreisel 2002), and in *ab initio* computer simulations of  $RAIO_3$  ( $R = La, Nd, Sm,$  and  $Gd$ ) and  $LaGaO_3$  at higher pressures (Tohei *et al* 2005). However, a powder XRD study suggested that pressure induces a first-order phase transition from  $R\bar{3}c$  to  $Imma$  symmetry in  $PrAlO_3$  perovskite (Kennedy *et al* 2002). The question therefore arises as to whether  $PrAlO_3$  is an exception to the general rules governing compression of perovskites (Zhao *et al* 2004a), or whether factors other than octahedral tilting contribute to the high-pressure behavior. In this contribution, we report a high-pressure structural study of  $PrAlO_3$  by high-resolution single-crystal x-ray diffraction that resolves this issue.

## 2. Experimental method

A relatively large single crystal from a batch grown by the Czochralski method (Pawlak *et al* 2005) was polished to a plate about 23  $\mu\text{m}$  thick and cut into smaller pieces approximately 60  $\mu\text{m} \times 100 \mu\text{m}$  for high-pressure experiments. No twin domains were observed by optical microscopy. The absence of twins was confirmed by the observation of sharp and unsplit x-ray diffraction maxima. The unit-cell parameters and refined structure at ambient pressure are consistent with those previously reported (Howard *et al* 2000, Kennedy *et al* 2002).

The selected crystal (60  $\mu\text{m} \times 100 \mu\text{m} \times 23 \mu\text{m}$ ) was loaded on to the 600  $\mu\text{m}$  diameter culet of one anvil of an ETH diamond anvil cell (Miletich *et al* 2000). A 200  $\mu\text{m}$  thick T301 steel gasket was pre-indented to a thickness of 90  $\mu\text{m}$  and a hole ( $\varnothing = 300 \mu\text{m}$ ) was drilled in the center of the indented region. A 4:1 methanol:ethanol mixture served as the pressure-transmitting medium. A ruby sphere ( $\sim 20 \mu\text{m}$ ) and quartz

**Table 1a.** Unit-cell parameters of  $PrAlO_3$  perovskite at high pressure.

$P$ (GPa)	$a$ ( $\text{\AA}$ )	$c$ ( $\text{\AA}$ )	$V$ ( $\text{\AA}^3$ )
0.0001	5.333 13(16)	12.972 9(4)	319.544(19)
0.700(3)	5.326 87(12)	12.957 5(3)	318.417(20)
1.407(6)	5.320 51(15)	12.942 9(4)	317.298(19)
2.094(4)	5.314 56(10)	12.927 76(27)	316.219(12)
3.060(5)	5.306 47(13)	12.907 7(4)	314.769(16)
3.904(6)	5.299 57(12)	12.891 6(3)	313.560(15)
4.859(5)	5.291 69(10)	12.873 06(28)	312.178(13)
5.896(7)	5.283 49(15)	12.854 7(4)	310.768(18)
6.567(6)	5.278 29(21)	12.842 9(6)	309.871(26)
6.965(7)	5.275 53(23)	12.835 75(23)	309.374(28)

crystal were loaded together with the crystal as the internal pressure calibrants (Angel *et al* 1997, Mao *et al* 1986). All unit-cell parameters up to  $\sim 7$  GPa (table 1a) were determined by a least-squares fit to the corrected setting angles of 15–20 reflections measured by the eight-position centering technique (Angel *et al* 1997) on a Huber four-circle diffractometer.

Intensity data for all accessible reflections were collected at room pressure (in air and in the DAC) and at different pressures for the sample using  $\omega$  scans in the fixed- $\varphi$  mode (Finger and King 1978) from  $2^\circ$  to  $40^\circ$  in  $\theta$  on an Xcalibur-I diffractometer (Oxford Diffraction) with  $Mo K\alpha$  radiation and a point detector. The offsets of the crystal from the rotation axis of the goniometer were determined by measuring twenty to forty strong low-angle reflections and calculating the crystal offsets from the reflection positions with the WinIntegrStp program, v3.5 (Angel 2003). These offsets were minimized by adjusting the DAC on the goniometer before data collection. Peak fitting and integration of data collection scans were carried out with the WinIntegrStp 3.5 software. Other data corrections including absorption by the sample itself, the diamond anvils and the beryllium plates of the DAC as well as shadowing by the gasket were made by ABSORB 6.0 (Angel 2004). After the crystallographically equivalent reflections were averaged, the remaining independent reflections with ( $F^2 > 2\sigma(F^2)$ ) were used to refine structures with RFINE99, a development version of RFINE4 (Finger and Prince 1975). Unit-cell parameters measured on the Huber diffractometer were used in the structure refinements. Refinement information and parameters for the sample in the DAC at ambient pressure are listed in tables 1a and 2a–2c. A second set of high-pressure experiments was subsequently performed with a second loading of the same crystal, in order to investigate the previously reported phase transition above 7 GPa.

For Raman measurements another piece of the  $PrAlO_3$  crystal was loaded along with a ruby ball as the pressure marker into a BR-series DAC (High-Pressure Diamond Optics, Inc) with a 4:1 methanol:ethanol mixture as the pressure medium. The sample was not oriented and unpolarized Raman spectra were then collected in backscattering geometry at room temperature and several pressures with a Jobin-Yvon Horiba LabRam HR800 system, equipped with an electronically cooled charge coupled device (CCD) detection system ( $1024 \times 256$ ) and a grating with 2400 grooves  $\text{mm}^{-1}$ . The laser beam, emitted from a Laser-physics Reliant 100S-514 nm argon

**Table 1b.** Bulk moduli of unit-cell volume, axes, and  $\text{AlO}_6$  and  $\text{PrO}_{12}$  polyhedra.

BM EoS fit	$K_0$ (GPa)	$K'$	$P_{\max}$ (GPa)	$\chi^2$
$V_0 = 313.559(9) \text{ \AA}^3$	193.0(1.2)	6.6(4)	0.016	0.5
$a_0 = 5.333\ 14(12) \text{ \AA}$	195.0(2.0)	5.5(6)	0.024	0.4
$c_0 = 12.973\ 19(29) \text{ \AA}$	189.8(1.9)	8.7(6)	0.033	1.0
$V_{\text{PrO}_{12}} = 44.08(5) \text{ \AA}^3$	220(15)	4(fixed)	0.8	0.51
$V_{\text{AlO}_6} = 9.106(9) \text{ \AA}^3$	182(9)	4(fixed)	0.7	1.08

laser with an output power of 50 mW, was focused onto the sample by an Olympus 10 $\times$  objective. The laser power at the sample was estimated to be about 3 mW. The width of the monochromator entrance slit was 150  $\mu\text{m}$ .

### 3. Results and discussion

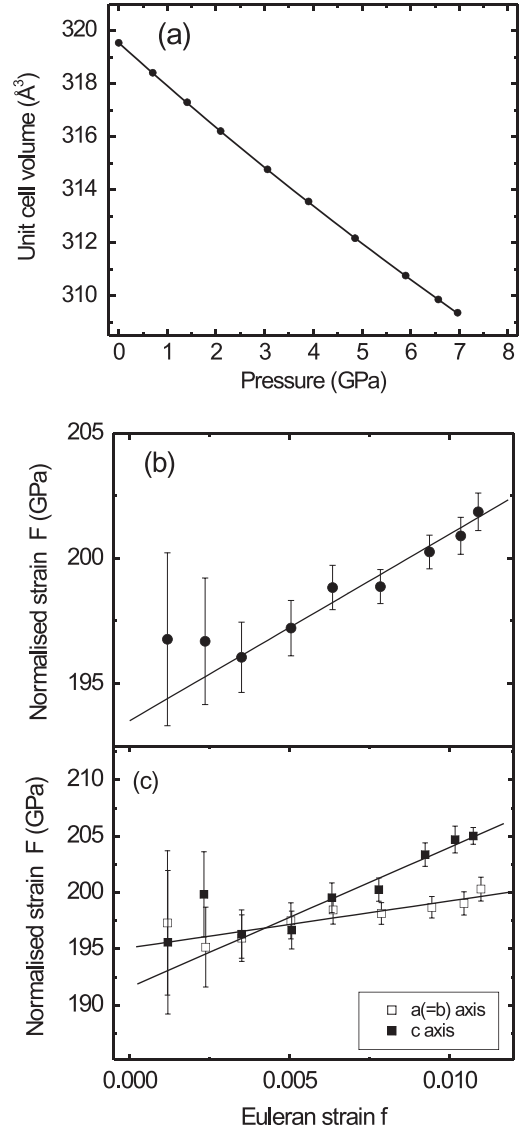
This section consists of three parts. We first present the elasticity of  $\text{PrAlO}_3$ , the bulk modulus, and the axial bulk moduli, and then we examine the variation of the spontaneous strains with pressure. In section 3.2 we present the structural evolution of  $\text{PrAlO}_3$ , paying special attention to the relative compressibilities of the  $\text{AlO}_6$  and  $\text{PrO}_{12}$  polyhedra, the tilt angle of octahedral  $\text{AlO}_6$  and the polyhedral distortions with increasing pressure. Finally the evidence for a high-pressure phase transition is presented.

#### 3.1. Equation of state of $\text{PrAlO}_3$ and lattice strains

The unit-cell volume of  $\text{PrAlO}_3$  perovskite decreases smoothly as a function of pressure without evidence of any phase transition before 7 GPa as shown in figure 1(a), consistent with the high-pressure powder x-ray diffraction data (Kennedy *et al* 2002). A least-squares fit of the  $P$ - $V$  data with a third-order Birch–Murnaghan equation of state (EoS) yielded a room pressure bulk modulus of  $K_0 = 193.0 \pm 1.2$  GPa and  $K' = (dK/dP)_{P=0} = 6.6 \pm 0.4$  (table 1b and figure 1(b)). The value of  $K'$  is typical of many oxide perovskites (Angel *et al* 2007, Ross *et al* 2004a, 2004b).

We obtained the compressional moduli of the unit-cell axes ( $a = b, c$ ) of  $\text{PrAlO}_3$  perovskite by fitting a third-order Birch–Murnaghan equation of state to the cubes of  $a$ - and  $c$ -axial lengths (Angel 2000). At room pressure  $\text{PrAlO}_3$  is almost elastically isotropic, with  $K_{a0} = 195.0(2.0)$  GPa being very slightly stiffer than  $K_{c0} = 189.8(1.9)$  GPa. As a consequence the ratio  $c/a\sqrt{6}$ , which expresses the deviation from cubic lattice symmetry, remains essentially constant at low pressures (figure 2). But at higher pressures, the fact (table 1b and figure 1(c)) that  $K'_{c0} = 8.7(6)$  is higher than  $K'_{a0} = 5.5(5)$ , means that the  $c$ -axis becomes stiffer than the  $a$ -axis and the ratio  $c/a\sqrt{6}$  increases, but at a much slower rate than that observed in the  $R\bar{3}c$  perovskite  $\text{LaAlO}_3$  (figure 2) in which the  $c$ -axis is significantly stiffer than the  $a$ -axis (Zhao *et al* 2004b).

A complete analysis of the possible phase transitions in  $\text{PrAlO}_3$  has been made within the framework of Landau theory (Carpenter *et al* 2005) which shows that the spontaneous strain provides the principal coupling between the order



**Figure 1.** (a) Variation of the unit-cell volume of  $\text{PrAlO}_3$  as a function pressure. The line is the third-order Birch–Murnaghan EoS fit to the data. (b) Normalized stress–strain plot derived from the measured  $P$ - $V$  data and the Birch–Murnaghan EoS. (c) Normalized stress–strain plots from the measured cell parameters and the Birch–Murnaghan EoS. In parts (b) and (c) the slopes of the  $f$ - $F$  plots of the data are equal to  $\frac{2}{3}K_0(K' - 4)$  (Angel 2000).

parameters representing the possible distortions of the structure. The spontaneous strain components for the possible phase transitions in  $\text{PrAlO}_3$  can be specified relative to the aristotype structure with  $Pm\bar{3}m$  symmetry. It is more convenient for these calculations to be performed on the pseudo-cubic rhombohedral setting of the unit-cell, in which  $a = b = c$  and  $\alpha = \beta = \gamma$ . The pseudo-cubic cell is related to the hexagonal cell by the vector equations:

$$\begin{aligned}
 \mathbf{a}_{\text{pc}} &= -\frac{2}{3}\mathbf{a}_{\text{hex}} - \frac{1}{3}\mathbf{b}_{\text{hex}} + \frac{1}{6}\mathbf{c}_{\text{hex}} \\
 \mathbf{b}_{\text{pc}} &= +\frac{1}{3}\mathbf{a}_{\text{hex}} - \frac{1}{3}\mathbf{b}_{\text{hex}} + \frac{1}{6}\mathbf{c}_{\text{hex}} \\
 \mathbf{c}_{\text{pc}} &= +\frac{1}{3}\mathbf{a}_{\text{hex}} + \frac{2}{3}\mathbf{b}_{\text{hex}} + \frac{1}{6}\mathbf{c}_{\text{hex}}.
 \end{aligned}
 \tag{4}$$

**Table 2a.** Refinement information for PrAlO<sub>3</sub> at high pressure.

P (GPa)	0.0001	0.700(3)	1.407(6)	2.094(4)	3.060(5)	3.904(6)	4.859(5)	5.896(7)	6.965(7)
$N(I > 2I_0/\sigma(I_0))^a$	321	307	305	319	313	310	303	284	291
$N(F^2 > 2\sigma(F^2))^b$	79	87	87	91	87	86	86	86	86
$R_{\text{int}}^c$	0.030	0.033	0.043	0.037	0.043	0.046	0.047	0.044	0.042
$G_{\text{fit}}^d$	1.05	1.20	1.14	1.07	0.90	0.94	1.08	1.11	0.95
Extinction factor ( $\times 10^{-4}$ )	0.63(7)	0.71(8)	0.57(8)	0.58(6)	0.55(6)	0.53(6)	0.62(9)	0.49(7)	0.48(5)
$R_w^e$	0.036	0.040	0.040	0.038	0.032	0.035	0.040	0.040	0.035
$R_u^f$	0.028	0.029	0.031	0.028	0.025	0.027	0.029	0.027	0.024

<sup>a</sup> Number of reflections with  $I > 2I_0/\sigma(I_0)$ .

<sup>b</sup> Number of independent reflection with  $F^2 > 2\sigma(F^2)$ .

<sup>c</sup> Internal residual for symmetry-equivalent intensities.

<sup>d</sup> Estimated standard deviation of unit weight observation.

<sup>e</sup> Weighted  $R_w = [\sum w(|F_0| - |F_c|)^2 / \sum |F_0|^2]^{1/2}$ , weight  $w = [\sigma_i^2(F_i) + p^2 F_i^2]^{-2}$ .

<sup>f</sup> Unweighted  $R_u = \sum ||F_0| - |F_c|| / \sum |F_0|$ .

**Table 2b.** Refined positional parameters and anisotropic temperature factors and equivalent isotopic temperature factors ( $B_{\text{eq}}$ ) of PrAlO<sub>3</sub> perovskite at high pressure.

P (GPa)	0.0001	0.700(3) <sup>a</sup>	1.407(6)	2.094(4) <sup>a</sup>	3.060(5)	3.904(6) <sup>a</sup>	4.859(5)	5.896(7)	6.965(7) <sup>a</sup>
Pr <sup>b</sup>									
$B_{\text{eq}}$	0.34(4)	0.39(4)	0.44(4)	0.35(3)	0.37(3)	0.36(3)	0.40(4)	0.37(4)	0.35(3)
$\beta_{11}$	0.0040(6)	0.0045(5)	0.0045(7)	0.0033(5)	0.0036(5)	0.0036(5)	0.0036(6)	0.0033(6)	0.0032(5)
$\beta_{33}$	0.00050(10)	0.00061(10)	0.00082(12)	0.00073(10)	0.00075(9)	0.00070(9)	0.00089(11)	0.00084(11)	0.00075(9)
Al <sup>c</sup>									
$B_{\text{eq}}$	0.36(9)	0.48(11)	0.56(11)	0.50(10)	0.57(9)	0.51(10)	0.51(11)	0.61(12)	0.49(10)
$\beta_{11}$	0.0061(17)	0.0057(19)	0.0061(19)	0.0050(18)	0.0060(15)	0.0070(17)	0.0033(18)	0.0050(18)	0.0044(16)
$\beta_{33}$	0.0000(5)	0.0006(6)	0.0010(6)	0.0010(6)	0.0010(5)	0.0006(6)	0.0015(6)	0.0015(7)	0.0011(6)
O <sup>d</sup>									
$x$	0.5477(14)	0.5459(15)	0.5477(16)	0.5463(14)	0.5458(12)	0.5457(12)	0.5433(15)	0.5446(15)	0.5429(12)
$B_{\text{eq}}$	0.43(12)	0.43	0.60(12)	0.43	0.49(13)	0.43	0.41(15)	0.39(14)	0.43
$\beta_{11}$	0.0038(15)	0.0038	0.0072(18)	0.0038	0.0031(15)	0.0038	0.0026(18)	0.0021(19)	0.0038
$\beta_{22}$	0.002(3)	0.002	0.002(3)	0.002	0.011(4)	0.002	0.005(4)	0.006(4)	0.002
$\beta_{33}$	0.0011(4)	0.0011	0.0013(5)	0.0011	0.0007(4)	0.0011	0.0010(5)	0.0009(5)	0.0011
$\beta_{23}$	0.0004(6)	0.0004	-0.0016(8)	0.0004	-0.0008(7)	0.0004	-0.0015(9)	-0.0007(9)	0.0004

<sup>a</sup> Anisotropic temperature factors  $\beta_{ij}$  of oxygen at room pressure were used and fixed in refinements.

<sup>b</sup> Pr:  $x = 0.0$ ,  $y = 0.0$ ,  $z = 0.25$ ,  $\beta_{22} = \beta_{11}$ ,  $\beta_{12} = 0.5\beta_{11}$ ,  $\beta_{13} = \beta_{23} = 0$ .

<sup>c</sup> Al:  $x = 0.0$ ,  $y = 0.0$ ,  $z = 0.0$ ,  $\beta_{22} = \beta_{11}$ ,  $\beta_{12} = 0.5\beta_{11}$ ,  $\beta_{13} = \beta_{23} = 0$ .

<sup>d</sup> O:  $x$ ,  $y = 0.0$ ,  $z = 0.25$ ,  $\beta_{12} = 0.5\beta_{22}$ ,  $\beta_{13} = 0.5\beta_{23}$ .

**Table 2c.** Interatomic distance and tilting angles of PrAlO<sub>3</sub> at high pressure.

P (GPa)	0.0001	0.700(3)	1.407(6)	2.094(4)	3.060(5)	3.904(6)	4.859(5)	5.896(7)	6.965(7)
Al–O ( $\text{\AA}^3$ ) $\times 6$	1.8983(10)	1.8949(10)	1.8939(11)	1.8907(10)	1.8875(8)	1.8850(10)	1.8807(10)	1.8787(10)	1.8748(7)
Pr–O <sub>1</sub> ( $\text{\AA}$ ) $\times 3$	2.412(7)	2.419(8)	2.406(9)	2.411(7)	2.410(6)	2.407(6)	2.417(8)	2.406(7)	2.411(6)
Pr–O <sub>21</sub> ( $\text{\AA}$ ) $\times 3$	2.921(7)	2.908(8)	2.914(9)	2.903(7)	2.896(6)	2.892(6)	2.875(8)	2.878(7)	2.864(6)
Pr–O <sub>22</sub> ( $\text{\AA}$ ) $\times 6$	2.6663(7)	2.6624(7)	2.6602(8)	2.6564(7)	2.6521(6)	2.6487(8)	2.6437(7)	2.6404(7)	2.6357(5)
O–Al–O (deg)	90.78(3)	90.74(3)	90.77(3)	90.75(3)	90.74(2)	90.73(3)	90.68(3)	90.70(3)	90.67(2)
$\omega$ (deg)	9.69(31)	9.34(31)	9.69(31)	9.38(27)	9.25(23)	9.23(23)	8.81(28)	9.06(27)	8.67(21)
$V_{\text{Al-act}}$ ( $\text{\AA}^3$ )	9.071(18)	9.069(16)	9.055(17)	9.010(14)	8.964(12)	8.928(12)	8.867(14)	8.839(14)	8.784(10)
$V_{\text{Pr-poly}}$ ( $\text{\AA}^3$ )	43.91(10)	44.00(9)	43.83(10)	43.69(8)	43.50(7)	43.33(7)	43.16(8)	42.95(8)	42.78(6)
$\eta$	0.9798	0.9807	0.9798	0.9805	0.9808	0.9809	0.9822	0.9816	0.9825

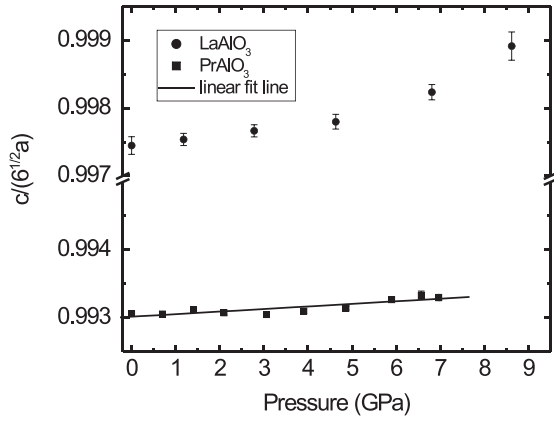
In this setting, the spontaneous strain components are then (Carpenter *et al* 2005):

$$e_1 = e_2 = e_3 = a_{\text{pc}}/a_0 - 1 \quad (5)$$

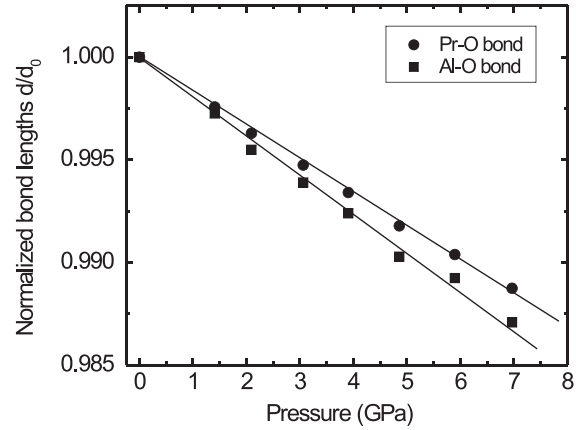
$$e_4 = e_5 = e_6 = \frac{a_{\text{pc}} \cos \alpha_{\text{pc}}}{a_0}. \quad (6)$$

The spontaneous strain components  $e_1 = e_2 = e_3$  are purely non-symmetry breaking for the  $Pm\bar{3}m$  to  $R\bar{3}c$

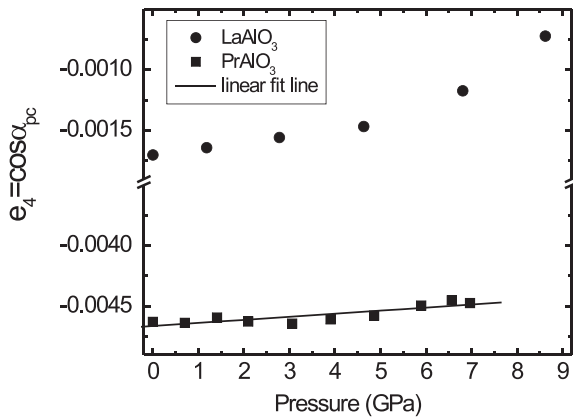
transition, but they cannot be evaluated at high pressure because we have no basis with which to estimate  $a_0$ . The components  $e_4 = e_5 = e_6$  are symmetry breaking. In the absence of a value for  $a_0$ , we make the approximations  $e_4 = e_5 = e_6 \approx \cos \alpha_{\text{pc}}$ , which are then purely symmetry breaking. The value of  $e_4$  for PrAlO<sub>3</sub> is further from zero than that for LaAlO<sub>3</sub>, confirming that the  $R\bar{3}c$  phase of PrAlO<sub>3</sub> deviates further from cubic symmetry. The slope of  $e_4$  with pressure is  $+2.5 \pm 0.5 \times 10^{-5} \text{ GPa}^{-1}$  (figure 3) which confirms



**Figure 2.** Variation of the ratio of unit-cell parameters  $c/a\sqrt{6}$  of  $\text{LaAlO}_3$  (top) and  $\text{PrAlO}_3$  (bottom) with pressure.



**Figure 4.** Variation of normalized average Al–O and Pr–O bond lengths of  $\text{PrAlO}_3$  as a function of pressure.

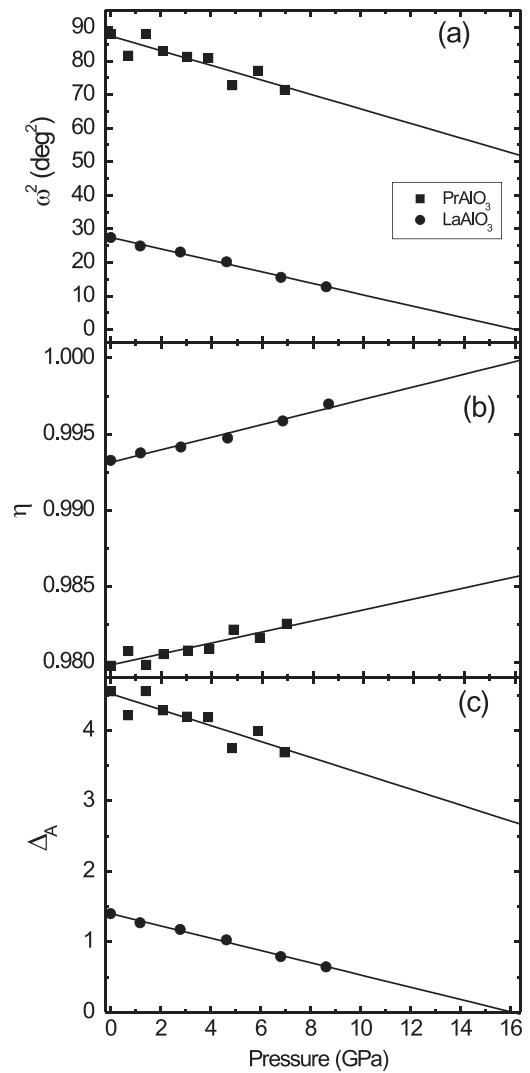


**Figure 3.** Variation of the spontaneous strain  $e_4$  of  $\text{LaAlO}_3$  (top) and  $\text{PrAlO}_3$  (bottom) with pressure. The line is a straight-line fit to the data, and has a slope of  $2.5(5) \times 10^{-5} \text{ GPa}^{-1}$ .

that the unit-cell of  $\text{PrAlO}_3$  evolves towards a cubic metric with increasing pressure. Figure 3 shows that this evolution is slower in  $\text{PrAlO}_3$  than in  $\text{LaAlO}_3$ .

### 3.2. Structural evolution of $\text{PrAlO}_3$

As expressed in equation (3), the key factor that determines the structural evolution of  $\text{PrAlO}_3$  is the relative compressibility of the Al–O and Pr–O bonds. The variations of the Al–O bond length and average Pr–O bond length with increasing pressure are shown in figure 4. The mean linear compressibilities  $\beta_{ij}$  ( $i = \text{Al, Pr}$  and  $j = \text{O}$ ) of both polyhedra are calculated using relation  $-1/R_{ij}(0) dR_{ij}/dP$ , where  $R_{ij}(0)$  is the average bond length at room pressure and  $dR_{ij}/dP$  is the slope of the average bond length. The Al–O bond ( $\beta_{\text{AlO}} = 1.81(8) \times 10^{-3} \text{ GPa}^{-1}$ ) is more compressible than the average Pr–O bond ( $\beta_{\text{PrO}} = 1.61(22) \times 10^{-3} \text{ GPa}^{-1}$ ). This is consistent with the bulk modulus of octahedral  $\text{AlO}_6$  being smaller than polyhedral  $\text{PrO}_{12}$  (see table 1b). As a consequence, the tilt angle  $\omega$  of the  $\text{AlO}_6$  octahedra decreases with pressure (figure 5(a)), as it does for  $\text{LaAlO}_3$  perovskite (Zhao *et al* 2004b). Linear extrapolation of the square of the tilt angle to zero suggests that the transition from  $R\bar{3}c$  to  $Pm\bar{3}m$  might occur at  $39 \pm 3 \text{ GPa}$ . The previous report of the octahedra being stiffer than the  $\text{PrO}_{12}$  polyhedra



**Figure 5.** (a) The tilt angle  $\omega^2$ , (b) and (c) distortion parameters  $\eta$  and  $\Delta_A$  of  $\text{PrAlO}_3$  and  $\text{LaAlO}_3$  as a function of pressure. Lines are the linear least-square fits to the data.

in  $\text{PrAlO}_3$  (figure 4(a) in (Kennedy *et al* 2002)), even though the tilt angle  $\omega$  decreases, appears to be the result of an error in calculation.

Other structural parameters of PrAlO<sub>3</sub> also evolve towards cubic symmetry with increasing pressure. The strain parameter  $\eta = c \cos \omega / a \sqrt{6}$  (e.g. Megaw and Darlington 1975, Thomas 1996) was introduced to describe the octahedral distortion. A value of  $\eta > 1$  indicates that the octahedra are elongated along the threefold rotation axis, whereas if  $\eta < 1$ , they are compressed. A value of  $\eta = 1$  corresponds to the completely regular octahedra found in the cubic aristotype structure. The strain parameter  $\eta$  of PrAlO<sub>3</sub> increases with pressure towards more regular octahedra (figure 5(b)) similar to LaAlO<sub>3</sub> perovskite. The distortion of the PrO<sub>12</sub> polyhedron can be quantified by:

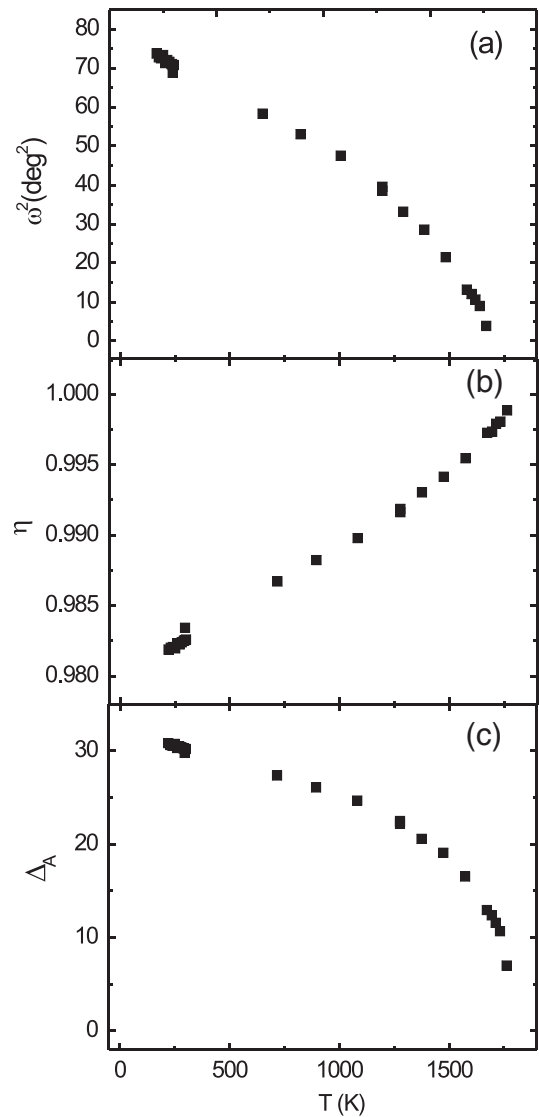
$$\Delta_i = (10^3/n) \sum \{(R_{ij} - \langle R_i \rangle) / \langle R_i \rangle\}^{1/2} \quad (7)$$

in which  $\langle R_i \rangle$  is the average bond length,  $R_{ij}$  is an individual bond length and  $n$  is the number of bonds (Sasaki *et al* 1983). The value for PrAlO<sub>3</sub> decreases towards the value of zero expected for the regular coordination that would be found in the cubic structure (figure 5(c)).

At ambient pressure the  $R\bar{3}c$  phase of PrAlO<sub>3</sub> is stable between 215 K, below which it transforms to a structure with *Imma* symmetry, and 1864(30) K above which it is expected to become cubic,  $Pm\bar{3}m$  (Carpenter *et al* 2005, Howard *et al* 2000). Over this entire temperature range the structure evolves towards cubic symmetry with decreasing octahedral tilts, and decreasing structural distortions with increasing temperature (figure 6, (Carpenter *et al* 2005, Howard *et al* 2000)). The evolution of the  $R\bar{3}c$  structure of PrAlO<sub>3</sub> with increasing pressure is thus the same as that with increasing temperature (Angel 2000), with a 40 K temperature change resulting in approximately the same change in the square of the tilt angle as a 1 GPa change in pressure. This is very similar to LaAlO<sub>3</sub>, for which  $dT/dP$  is 35 K GPa<sup>-1</sup>.

### 3.3. High-pressure phase transition

It has been reported, on the basis of powder diffraction, that PrAlO<sub>3</sub> undergoes a phase transition from  $R\bar{3}c$  to *Imma* at a pressure between 7.14 and 8.05 GPa (Kennedy *et al* 2002). In our experiments, the compression of single crystals above 7.5 GPa leads to irreversible broadening of the x-ray diffraction maxima. The geometry of the experiment allows us to exclude bridging of the anvils by the sample as the cause of this broadening, and the pressure medium remains hydrostatic to 10 GPa (Angel *et al* 2006). The reflections would not be broadened by a transition to cubic  $Pm\bar{3}m$  symmetry, and there is no mechanism other than a phase transition that would generate domains within the homogeneous crystal. We therefore attribute the reflection broadening to a reduction of symmetry and the formation of multiple twin domains within the former single crystal as a result of the transition reported by Kennedy *et al* (2002). It is not possible to independently establish the symmetry of the high-pressure phase from our experimental data, but several observations are consistent with the interpretation of the powder data (Kennedy *et al* 2002) that it has the same *Imma* symmetry as the low-temperature phase. A careful survey of reciprocal space with an area detector showed that there are no additional reflections. This eliminates



**Figure 6.** (a) The rotation angle  $\omega^2$ , (b) and (c) distortion parameters  $\eta$  and  $\Delta_A$  of PrAlO<sub>3</sub> as a function of temperature. Calculated from data in Howard *et al* (2000).

the possible space groups (Carpenter *et al* 2005)  $P4/mmm$ ,  $Pmmm$ , and  $C2/m$ , but is consistent with a change in lattice from *R* to *I*-orthorhombic, as this results in the same topology of lattice points. Refinements to the intensity data collected above the phase transition can be successfully completed in  $R\bar{3}c$  symmetry, indicating that the structural distortions from an average structure with  $R\bar{3}c$  symmetry are small, at least within 0.2 GPa of the transition. This also explains why we did not observe the violations of the *c*-glide diffraction condition that would be expected after a transformation to *Imma* symmetry. When the diffraction pattern of the high-pressure phase is indexed on the rhombohedral cell it shows, relative to the true  $R\bar{3}c$  unit-cell just below the transition, a small contraction in the *a* cell parameter and an expansion in the *c* cell parameter. Thus the pattern of spontaneous strain is the same as that observed at the  $R\bar{3}c$  to *Imma* transition at low temperature (Carpenter *et al* 2005). The reflection broadening, unfortunately, prevents the measurement of unit-

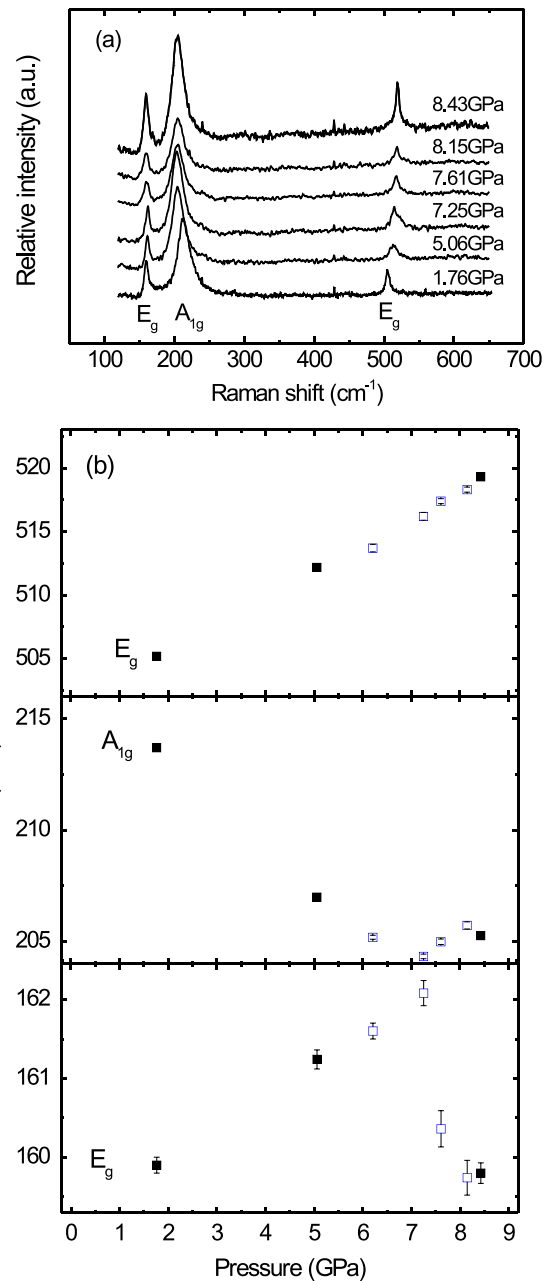
cell parameters to sufficient precision that would allow the determination of the thermodynamic character of the reported transition (Kennedy *et al* 2002).

On the basis of factor group analysis, five Raman-active modes of  $R\bar{3}c$  group of perovskite,  $A_{1g} + 4E_g$ , have been assigned (Harley *et al* 1973, Scott 1969). This is consistent with experimental Raman spectra of rhombohedral  $\text{LaAlO}_3$  (Bouvier and Kreisel 2002, Scott 1969),  $\text{NdAlO}_3$  (Scott 1969), and  $\text{PrAlO}_3$  (Harley *et al* 1973). Figure 7(a) shows the Raman spectra of  $\text{PrAlO}_3$  from 1.76 to 8.43 GPa. Three Raman modes of the  $R\bar{3}c$  phase of  $\text{PrAlO}_3$  (labeled in figure 7(a)) were identified. The  $E_g$  mode below  $100\text{ cm}^{-1}$  could not be recognized due to the high background from Rayleigh scattering. Figure 7(b) shows the change of the Raman shift of these three bands as a function of pressure. The Raman mode  $A_{1g}$  that is related to the tilt of the  $\text{AlO}_6$  octahedra (Harley *et al* 1973), and is initially at  $213\text{ cm}^{-1}$ , softens continuously as pressure is increased from room pressure up to 7 GPa, which is similar to the  $A_{1g}$  mode of  $\text{LaAlO}_3$  with both increasing pressure (Bouvier and Kreisel 2002) and temperature (Scott 1969). This is consistent with a decrease in the octahedral tilt angle with pressure (figure 5(a)). However, unlike  $\text{LaAlO}_3$  whose  $A_{1g}$  mode softens towards zero as the  $R\bar{3}c$  phase continuously evolves towards  $Pm\bar{3}m$  symmetry (Bouvier and Kreisel 2002), the  $A_{1g}$  mode of  $\text{PrAlO}_3$  hardens above 7.5 GPa following the phase transition (figure 7(b)), indicating that the decrease in the octahedral tilt towards the cubic phase has been interrupted. The  $E_g$  Raman mode around  $160\text{ cm}^{-1}$ , related to in-plane Pr and O shifts in the  $R\bar{3}c$  phase (Harley *et al* 1973) hardens below 7 GPa (figure 7(b)) and then begins to soften above 7 GPa. This is similar to the temperature-induced variation of the same Raman mode at room pressure that hardens as temperature is decreased, but softens below the phase transition to the  $Imma$  phase (Harley *et al* 1973). The changes in the Raman spectra at high pressures therefore mimic quite closely those associated with the low-temperature phase transition in  $\text{PrAlO}_3$  perovskite (Birgeneau *et al* 1974, Lyons *et al* 1975, Watanabe *et al* 2006).

#### 4. Conclusions

This structural study confirms that with increasing pressure the unit-cell and structure of  $\text{PrAlO}_3$  both initially evolve towards the ideal perovskite structure with  $Pm\bar{3}m$  symmetry, as do other perovskites with +3 cations (Angel *et al* 2007, Ross *et al* 2004a, 2004b). However,  $\text{PrAlO}_3$  is more distorted than  $\text{LaAlO}_3$  at room condition and it evolves more slowly towards the cubic phase than  $\text{LaAlO}_3$ . This is because the site compressibility parameter  $M_A/M_B$  for  $\text{PrAlO}_3$  is 1.18 at room conditions, meaning that the  $\text{PrO}_{12}$  and  $\text{AlO}_6$  polyhedra have very similar compressibilities as observed. By contrast  $M_A/M_B = 1.34$  for  $\text{LaAlO}_3$  (Zhao *et al* 2004b), and the structure evolves more rapidly towards cubic symmetry because the  $\text{AlO}_6$  octahedra are significantly softer in this material.

The two  $R\bar{3}c$  perovskites  $\text{PrAlO}_3$  and  $\text{LaAlO}_3$  also behave essentially identically from the thermodynamic point of view. Our estimate of  $39 \pm 3$  GPa for the pressure of the  $R\bar{3}c$



**Figure 7.** (a) Raman spectra of  $\text{PrAlO}_3$  at different pressures; (b) changes of the Raman band positions with increasing pressure. Open symbols represent data measured during decompression from the maximum pressure.

to  $Pm\bar{3}m$  phase transition at room temperature in  $\text{PrAlO}_3$ , together with the transition temperature of  $1864 \pm 30$  K at room pressure (Carpenter *et al* 2005, Howard *et al* 2000), yields a slope for the  $R\bar{3}c = Pm\bar{3}m$  phase boundary  $dT_c/dP_c = -40 \pm 4$  K  $\text{GPa}^{-1}$ . The slope for  $\text{LaAlO}_3$  is  $-35 \pm 3$  K  $\text{GPa}^{-1}$ . At temperatures in excess of the saturation temperature, the slope of the phase boundary is directly related to the strength of the coupling coefficient,  $\lambda$ , between the tilts of the octahedra and the volume strain (equation 46 in Carpenter 2007) as  $2\lambda/aK_c = dT_c/dP_c$  in which  $K_c$  is the bulk modulus of the cubic phase, and  $a$  the first coefficient in the Landau expansion



of the free energy with temperature (Carpenter 2007). Thus, the similarity in the slopes of the phase boundaries indicates that the microscopic mechanisms that drive the evolution of the structures of PrAlO<sub>3</sub> and LaAlO<sub>3</sub> with pressure, and the transitions, are essentially the same.

The single-crystal diffraction data and Raman data reported in this paper are consistent with the interpretation by Kennedy *et al* (2002) of high-pressure powder data that PrAlO<sub>3</sub> undergoes a transformation from  $R\bar{3}c$  to *Imma* at pressures in excess of 7 GPa. Given that, prior to the transition, the structure of PrAlO<sub>3</sub> evolves in the same way with *increasing* pressure as with *increasing* temperature, it is clear that the transition is not triggered by a critical value of the tilt of the octahedra, as they are becoming less tilted at high pressures, but more tilted at low temperatures. Instead, the driving force for the transition at high pressure must then simply be the reduction in volume associated with the transition to the *Imma* phase, that is also observed at low temperatures. The negative volume strain arises from the coupling between the electronic distortion and the tilting in the *Imma* phase (Carpenter and Howard 2009b, 2009a). The presence of an electronic component in this transition explains why it does not follow the general rules for pure tilt transitions in perovskites (Angel *et al* 2005).

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